

1. Basic Variables & kinematics equations



DEFINITIONS

LINEAR

ROTATIONAL / ANGULAR

$$x \quad (m) \quad \rightarrow \quad \theta \quad (\text{radians})$$

$$v = \frac{dx}{dt} \quad (m/s) \quad \rightarrow \quad \omega = \frac{d\theta}{dt} \quad (\text{rad/s})$$

$$a = \frac{dv}{dt} \quad (m/s^2) \quad \rightarrow \quad \alpha = \frac{d\omega}{dt} \quad (\text{rad/s}^2)$$

$$\bar{v} = \frac{\Delta x}{t} \quad \rightarrow \quad \bar{\omega} = \frac{\Delta \theta}{t}$$

DERIVED EQUATIONS (constant acceleration)

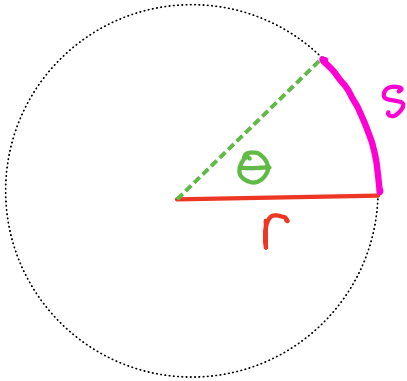
$$\bar{v} = \frac{v_i + v_f}{2} \quad \rightarrow \quad \bar{\omega} = \frac{\omega_i + \omega_f}{2}$$

$$x = \frac{1}{2}at^2 + v_i t + x_i \quad \rightarrow \quad \theta = \frac{1}{2}\alpha t^2 + \omega_i t + \theta_i$$

$$v = at + v_i \quad \rightarrow \quad \omega = \alpha t + \omega_i$$

$$v_f^2 = v_i^2 + 2a\Delta x \quad \rightarrow \quad \omega_f^2 = \omega_i^2 + 2\alpha\Delta\theta$$

2. Motion along a curved (circular) path



$$s = r\theta$$

- * radians are a dimensionless unit!
- * don't write it when mixed w/ linear stuff

$$v = r\omega$$

* Since $v = \frac{ds}{dt} = \frac{d(r\theta)}{dt} = r \frac{d\theta}{dt} = r\omega$

+ $v \rightarrow$ "linear speed"

+ $\omega \rightarrow$ "angular/rotational speed"

$$a_t = r\alpha$$

* $a_t =$ "tangential" acceleration

* $a_t = \frac{dv}{dt} \rightarrow$ the rate @ which object speeds up

$$a_r = r\omega^2$$

* $a_r =$ "radial" acceleration

a.k.a. centripetal acceleration

* $a_c = \frac{v^2}{r} = \frac{(r\omega)^2}{r} = r\omega^2$

NOTE: \vec{a}_t & \vec{a}_r are defined based on VELOCITY

a_t is \parallel to $\vec{v} \rightarrow$ changes magnitude of \vec{v}

a_r is \perp to $\vec{v} \rightarrow$ changes direction of \vec{v}